

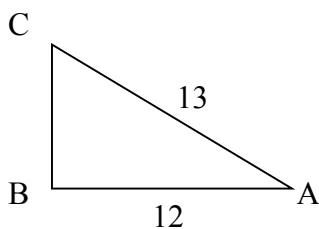
## ACT REVIEW PROBLEMS

1. Which of the following equations has  $y$  varying directly as the square of  $w$  and inversely as the cube of  $t$ ?
- A.  $\frac{y^2}{t^3} = w$     B.  $\frac{w^2}{t^3} = y$
- C.  $\frac{t^2}{w^3} = y$     D.  $\frac{\sqrt{w}}{\sqrt[3]{t}} = y$     E.  $\frac{w^2}{y^3} = t$
2. How many points do the graphs of all 3 of the following equations have in common?
- $-x = y - 3$   
 $-x = -y - 3$   
 $3x = -3y + 2$
- A. 0  
B. 1  
C. 2  
D. 3  
E. Infinitely many
3. Listed below are 5 functions, each denoted  $g(x)$  and each involving a real number constant  $c \geq 2$ . If  $f(x) = 2^x$ , which of these five functions yields the greatest value for  $f(g(x))$
- A.  $g(x) = c(x)$   
B.  $g(x) = \frac{c}{x}$   
C.  $g(x) = \frac{x}{c}$   
D.  $g(x) = x - c$   
E.  $g(x) = \log_c x$
4. If  $2x - y = 6$  and  $x + 4y = 12$ , what is the value of  $y$ ?
- A. -6  
B. 0  
C. 1  
D. 2  
E. 3
5. Which of the following is a factored form of  $4x^3y + 4xy^3$ ?
- A.  $4x^3y^3(y + x)$   
B.  $4xy(x^2 + y^2)$   
C.  $8xy(x^2 + y^2)$   
D.  $4x^3y^3$   
E.  $8x^4y^4$
6. You are told that  $m = ak + 5$  where  $a \neq 0$ . Which of the following equations expresses  $k$  in terms of  $a$  and  $m$ ?
- A.  $k = \frac{m-5}{a}$     B.  $k = \frac{5-m}{a}$
- C.  $k = \frac{m+5}{a}$     D.  $k = \frac{m}{a} - 5$     E.  $k = \frac{m}{a} + 5$
7. For all nonzero  $r$ ,  $t$ , and  $z$  values,  $\frac{16r^3tz^5}{-4rt^3z^2} = ?$
- A.  $-\frac{4z^3}{r^2t^2}$   
B.  $-\frac{4z^3}{r^2t^2}$   
C.  $-\frac{4z^3}{r^2t^2}$   
D.  $-4r^4t^4z^7$   
E.  $-4r^2t^{-2}z^3$
8. Which of the following conditions on  $x$  determines when  $(x-2)(x+3) - (x^2-4)$  will be positive?
- F.  $x = -2$   
G.  $x > 2$   
H.  $x \geq 10$   
I.  $2x^2 \geq 10$   
J.  $x^2 - x < 6$
9. If  $A$ ,  $B$ , and  $C$  are real numbers, and if  $ABC = 1$ , which of the following conditions **must** be true.
- F.  $AB$  is equal to  $\frac{1}{C}$   
G.  $A$ ,  $B$ ,  $C$  must all be positive  
H. Either  $A = 1$ ,  $B = 1$ , or  $C = 1$   
I. Either  $A = 0$ ,  $B = 0$ , or  $C = 0$   
J. Either  $A < 1$ ,  $B < 1$ , or  $C < 1$
10. For what value of  $a$  would the following system of equations have an infinite number of solutions?
- $$\begin{aligned} 2x - y &= 6 \\ 8x - 4y &= a \end{aligned}$$
- A. 2    B. 6    C. 8    D. 18    E. 24
11. Which of the following is a factor of  $x^2 - 5x - 6$ ?
- F.  $(x-1)$     G.  $(x+2)$     H.  $(x-2)$
- J.  $(x-3)$     K.  $(x-6)$
12. Which of the following identifies exactly those values of  $x$  that satisfy  $5 - 2(3-x) \geq 5x - 3(x-1)$
- A. All real numbers  
B.  $x \leq -1$     C.  $x \geq \frac{1}{2}$     D.  $x \leq \frac{1}{2}$
- E. No real numbers

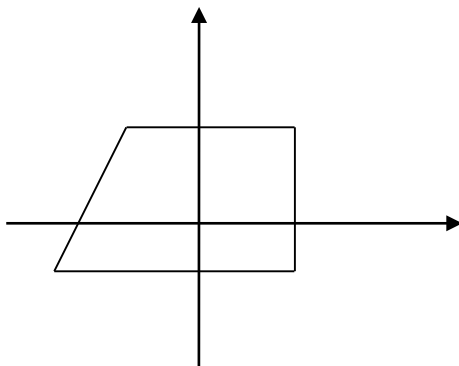
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- How many roots does the function  $f(x)$  have, if  $f(x) = (2x - 3)(4x + 4)(5x + 2)(x - 1)$ ?
- One angle,  $\angle A$ , has 3 times the measure of its supplement,  $\angle B$ . What is the degree measure of  $\angle A$ ?

- In the right triangle ABC below, what is the value of  $\sin A$ ? What is the value of  $\cos C$ ?



- What is the area, in square units, of the trapezoid graphed below?

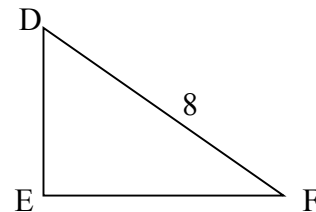
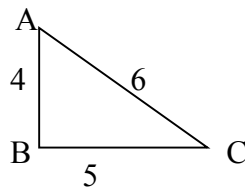


- Simplify:

a)  $\frac{a^{-2}}{b} (a^2 b^2) =$

b)  $\frac{x^2 y}{x^{-3} y^4} =$

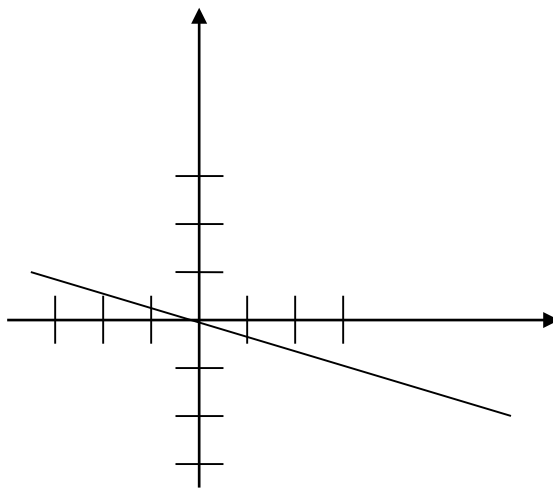
- The two triangles below are similar with  $\angle A \cong \angle D$ . What is the perimeter of  $\triangle DEF$ ?



- (Use diagram from question 6) What is the ratio of the area of  $\triangle ABC$  to the area of  $\triangle DEF$ ?

- Which of the following equations is graphed below?

- a)  $y = -3x$    b)  $y = (-\frac{1}{3})x$   
 c)  $y = (\frac{1}{3})x$    d)  $y = 3x$   
 e)  $y = x - 3$



- Write the equation of a circle with the center at the origin and radius 5m.

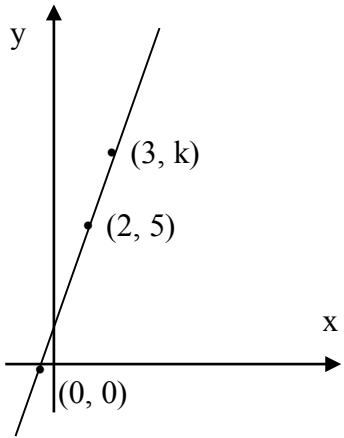
- What is the center of the circle described by the equation:  $(x - 5)^2 + (y + 3)^2 = 16$

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10. Write the equation of a circle with the center at  $(-4, -7)$  and radius  $\sqrt{5}$ .

11. In the  $(x, y)$  coordinate plane below, a straight line passes through the 3 indicated points. What is the value of  $k$ ?

- A.  $-\frac{15}{2}$     B.  $-\frac{6}{5}$   
 C.  $\frac{6}{5}$     D. 6  
 E.  $\frac{15}{2}$



12. In a laboratory experiment, Amoeba A lives 5 hours longer than Amoeba B, and Amoeba B lives twice as long as Amoeba C. If  $n$  is the lifespan of Amoeba C in hours, what is the lifespan of Amoeba A, in terms of  $n$ ?

- A.  $5 + 2n$     B.  $7 + n$     C.  $7n$   
 D.  $10n$     E.  $2(5 + n)$

13. If the denominator is NOT zero, then

$\frac{3X^2 - 3Y^2}{-X - Y}$  simplifies to:

- F.  $-3Y - 3X$   
 G.  $3Y - 3X$   
 H. 3  
 J.  $3X + 3Y$   
 K.  $3X - 3Y$

14. Which of the following polynomials has 0 and  $\frac{3}{4}$  as zeros?

- A.  $4x - 3$   
 B.  $4x + 3$   
 C.  $4x^2 + 3x$   
 D.  $4x^2 - 3x$   
 E.  $3x^2 - 4x$

15. The equation  $x^2 - 10x + k = 0$  has only one solution for  $x$ . What is the value of  $k$ ?

- A. 0    B. 5    C. 10    D. 20    E. 25

16. The graph of the solution set for the system of equations below is a single line in the standard  $(x, y)$  coordinate plane.

$$\begin{aligned} 18x - 30y &= 54 \\ 6x + ky &= 18 \end{aligned}$$

What must be the value of  $k$ ?

- A. -10    B. -6    C.  $-\frac{1}{3}$     D.  $\frac{3}{5}$     E. 3

17. In the standard  $(x, y)$  coordinate plane, what is the slope of the line that passes through the origin and the point  $(\frac{1}{2}, \frac{2}{3})$  \_\_\_\_\_

18. If  $x - y = 5$  and  $x + y = -4$ , what is the value of  $x^2 - y^2$  \_\_\_\_\_

19. What is the slope of any line parallel to the line  $3x + 5y = 8$ ? \_\_\_\_\_

# ACT I